

# CMS Analysis Note

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## Measurement of the CSC Spatial Resolution with Cosmic Ray Muons

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### Abstract

The spatial resolution of the CMS Cathode Strip Chambers (CSC) has been measured using cosmic ray data taken in 2008 (CRAFT) using an offline analysis package, `CSCResiduals`. The expected behavior with charge, high voltage, position within a strip, strip width and track inclination are established. The resolution *per layer* and *per chamber* are measured and found to be close to the design values, despite the fact the high voltage setting is somewhat lower than planned.



## 1 Introduction

The success of any CMS physics analysis involving muons depends on achieving the design performance of several sub-detector systems, including the Cathode Strip Chambers (CSC's) which are installed in the end cap regions. A large sample of cosmic ray muons was collected in the Fall of 2008, in preparation for data taking with collisions at the LHC. This cosmic ray data sample is commonly referred to as "CRAFT" (*Cosmic Run at Four Tesla*). The CMS apparatus, trigger and reconstruction software were all working well, providing the basis for detailed studies of the performance of many sub-detector systems, including the CSC's. The commissioning of the CSC's prior to CRAFT is documented in Ref. [1].

The CSC's have been described in detail elsewhere [2]. They measure the  $\phi$  coordinates of muon tracks well, as the bending of the muon trajectories in the magnetic fields is mainly about the  $\hat{s}$  direction, where  $\hat{s}$  is a unit vector in cylindrical coordinates pointing away from the beam line. The strips describe constant  $\phi$  values, and hence are trapezoidal in shape, like the chambers themselves. A high precision is achieved on the basis of the shape of the charge distribution on three consecutive strips; this allows an adequate measurement of the muon momentum as needed for triggering purposes.

The CRAFT data were used to study and measure the spatial resolution of the CSC's as they are meant to be operated for early physics<sup>1</sup>. The purpose of this study is to demonstrate that all working chambers perform as designed, before colliding beams commence. Excellent earlier studies of CSC spatial resolution can be found in Ref. [4, 5].

The following sections define what we mean by "resolution," and how we measured it. We show the expected variations of the resolution as functions of charge, position within a strip, the width of the strip, and angle. We report measured values of the resolution for all types of chambers, and then conclude.

## 2 Analysis

The reconstruction of muon trajectories and the measurement of the muon momentum depends critically on the spatial resolution of the chambers<sup>2</sup>. The most important coordinate is  $\phi$ , so these studies are concerned with the strip measurements only. An adequate measurement of  $R$  at a given  $z$  is given by the anode wires [2].

### 2.1 Methodology

It is important to define "resolution" and to state how it is to be measured. The *resolution* is the typical measurement error. It is determined by the design parameters of the chamber (width of the cathode strip, distance to the anode wire plane, high voltage, anode wire radius and pitch, gas mixture, electronics noise and cross talk) as well as certain characteristics of each muon track (angle, position with respect to the center of the struck strip, and amount of charge collected), and of course the physics of multi-wire proportional chambers (electron diffusion, magnetic field influence) and the reconstruction (reduction of data and knowledge of misalignments). The distribution of hit residuals with respect to the muon trajectory can

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<sup>1</sup>The current high voltage settings are intentionally lower than what was used for the test beam, in order to avoid aging the chambers unnecessarily during commissioning periods. This has a significant impact on the spatial resolution, as described below

<sup>2</sup>The reconstruction software, the chamber efficiency and the success of muon reconstruction are discussed elsewhere[6-9]

ring	chambers per ring	strips per chamber	strip width (mm)	(mrad)
ME±1/1a	36	48	4.11 – 5.82	3.88
ME±1/1b	36	64	4.44 – 7.6	2.96
ME±1/2	36	80	6.6 – 10.4	2.33
ME±1/3	36	64	11.1 – 14.9	2.16
ME±2/1	18	80	6.8 – 15.6	4.65
ME±2/2	36	80	8.5 – 16.0	2.33
ME±3/1	18	80	7.8 – 15.6	4.65
ME±3/2	36	80	8.5 – 16.0	2.33
ME±4/1	18	80	8.6 – 15.6	4.65

Table 1: selected relevant physical specifications of the cathode strip chambers. The ME±1/1 chambers have a split cathode, with 64 strips at larger radii, and 48 strips at smaller. For more information, see Ref. [2, 3]

52 give a good measure of the resolution. A *residual* is the difference between the measured  
53 coordinate and the true or estimated true (i.e., predicted) coordinate.

54 For the purposes of the study, the coordinate of interest is the coordinate measured by the  
55 strips. In global coordinates, this would be  $R\phi$  as measured in centimeters, but most of the  
56 studies are couched in *strip coordinates*. The strip coordinate,  $s$ , is the  $R\phi$  coordinate relative  
57 to the center of the strip divided by the strip width at the position of the hit. Modulo resolu-  
58 tion effects, one has  $-0.5 \leq s \leq 0.5$ . Most of the plots here will show residuals distributions  
59 in strip coordinates. In order to obtain a resolution in physical units, we multiply by the  
60 mean width of a strip in the given chamber.

The residuals distribution is not Gaussian, in general, so one must settle on a measure of the residuals distribution to be identified with the “resolution” of the given chamber. Usually we fit the distribution with a sum of two Gaussian functions, and if the resulting widths are  $\sigma_1$  and  $\sigma_2$ , and the areas of the two Gaussian functions are  $A_1$  and  $A_2$ , then we take the resolution to be:

$$\text{resolution : } \quad \bar{\sigma} = \sqrt{\frac{A_1\sigma_1^2 + A_2\sigma_2^2}{A_1 + A_2}}. \quad (1)$$

61 See also Appendix B. If one Gaussian suffices, then we take simply the  $\sigma$  parameter of the  
62 single Gaussian. We do not take the r.m.s. as the residual distributions often have long  
63 non-Gaussian tails which inflate the r.m.s. - these tails are caused by  $\delta$ -ray electrons and fall  
64 outside a discussion of the core resolution.

As defined, the resolution  $\bar{\sigma}$  pertains to a hit in a *single layer*. The resolution of a chamber is more complicated, since it depends on the number of hits in the segment, the angle of the segment, the generally non-normal angle between wire groups and strips, and the fact that the strips are staggered layer-by-layer<sup>3</sup>. We can take the special case of segments with six hits that are normal to the chamber and pass through the center. If the residuals distribution near the edge of a strip has Gaussian width  $\sigma_e$ , and near the center of a strip,  $\sigma_c$ , then to a good approximation, the resolution for the segment is

$$\text{segment : } \quad \sigma_{\text{seg}} = \left( \frac{3}{\sigma_e^2} + \frac{3}{\sigma_c^2} \right)^{-1/2}. \quad (2)$$

<sup>3</sup>There is no strip staggering in the ME1/1 chambers

65 We will use this expression to characterize the chamber resolution.

Another method for measuring the resolution does not rely on the residuals of a single layer, but rather on the value of  $\chi^2$  for the linear fit to all six hits. Let us define the *unweighted*  $\chi^2$  as follows:

$$\chi_0^2 \equiv \sum_{i=1}^6 (s_i - (a + bi))^2 \quad (3)$$

66 where  $a$  and  $b$  are free parameters, and  $i$  plays the role of the  $z$  coordinate. Notice we have set  
67 all uncertainties to one. As a consequence,  $\langle \chi_0^2 \rangle = 6\sigma_0^2$ , where  $\sigma_0$  is the effective uncertainty  
68 on  $s_i$ . This  $\sigma_0$  parameter can be interpreted as the resolution only if non-Gaussian tails in are  
69 absent or insignificant.

70 It remains to explain how we make the residuals distribution. We do not have a good exterior  
71 measure of the position of the muon, so we have to use the segment itself. Perhaps the  
72 cleanest procedure is to use five out of the six hits on a good segment to predict the position  
73 of the sixth. In practice, we fit the hits in layers 1, 2, 4, 5 and 6 to a straight line to predict the  
74 “correct” position in layer 3, and then compare to the measured position in layer 3. Monte  
75 Carlo studies show that the width of the residuals distribution is inflated by about 10% due  
76 to the measurement error from the five-hit fit; this uncertainty is larger for layers 1, 2, 5 or 6.  
77 We do not remove this 10% inflation in the results reported in this note.

## 78 2.2 Expected Behavior

79 As stated in the Introduction, the resolution varies with four quantities:

- 80 1. the charge recorded for that hit
- 81 2. the position within the strip
- 82 3. the physical width of the strip
- 83 4. the inclination of the track

84 This behavior can be understood qualitatively, given a model for the formation of signals on  
85 the strips.

86 Analytical calculations for the formation of signals in cathode strip chambers have been  
87 available for many years. Gatti described how charge was apportioned among the strips in  
88 1979 [10]. His calculation was updated and extended by Mathieson and Gordon in 1984 [11].

89 The simplest depiction of the signals on three strips as given in Fig. 1. Ignoring the time  
90 evolution of the pulses, we have simply  $Q_L$ ,  $Q_C$  and  $Q_R$ , as shown. By definition, the central  
91 strip extends across  $-0.5 < s < 0.5$ , and the left strip is at  $s = -1$  and the right, at  $s = +1$ .  
92 With the muon passing through the central strip at the position of the arrow,  $Q_R > Q_L$ , and  
93 of course  $Q_C > Q_R$ .

It is intuitively clear that the position of the muon relates to the relative difference  $Q_R - Q_L$ , and indeed the first approximation to this position is simply

$$s \approx \frac{1}{2} \frac{Q_R - Q_L}{Q_C - \min(Q_R, Q_L)}. \quad (4)$$

94 For a justification of this choice, see Ref. [4, 7].

95 The accuracy of the measurement of  $s$  depends on how well the difference  $Q_R - Q_L$  can be  
 96 measured. For the CSC's, most of the charge appears on the central strip, unless the muon  
 97 passes quite close to the edge of the strip. For the large chambers especially,  $Q_R$  and  $Q_L$  are  
 98 only a few percent of  $Q_C$ , and in the worse cases are not much larger than the pedestal width.  
 99 This width characterizes the electronics noise, so the central question is: are the observed  
 100 charges  $Q_R$  and  $Q_L$  larger than or comparable to this noise?

101 If the total charge  $Q$  is large, then the impact of the noise will be reduced. This explains why  
 102 the resolution improves as  $Q$  decreases, so long as  $\delta$ -ray electrons are not interfering with  
 103 the charge distribution. Explicit calculations show that the resolution should be proportional  
 104 to  $1/Q$  [10, 11].

The charge on the right strip will increase as the muon trajectory approaches  $s = 0.5$ . In the  
 limit that  $s \rightarrow 0.5$ ,  $Q_L$  does not matter, and the approximation in Eq. 4 becomes

$$s \approx \frac{1}{2} \frac{Q_R}{Q_C} \rightarrow \frac{1}{2}$$

105 since  $Q_R \rightarrow Q_C$  in this limit. In such a case, the electronics noise becomes relatively unim-  
 106 portant, since both  $Q_R$  and  $Q_C$  are substantial. In contradistinction, as the muon trajectory  
 107 approaches  $s = 0$ , both  $Q_L$  and  $Q_R$  are minimal and therefore maximally impacted by elec-  
 108 tronics noise, making the difference  $Q_R - Q_L$  relatively difficult to measure. For these rea-  
 109 sons, one expects the best resolution for muon trajectories close to the edge of the strip, and  
 110 the worst resolution when they go through the center.

111 The spatial distribution of the charge depends on the separation between strips, for a fixed  
 112 distance between the strip plane and the anode wire plane. If the physical width of the strip  
 113 is large, then  $Q_L$  and  $Q_R$  will be small. Due to the impact of electronics noise, which tends  
 114 to be larger when the strips are larger, the resolution is poorer in chambers with large strips

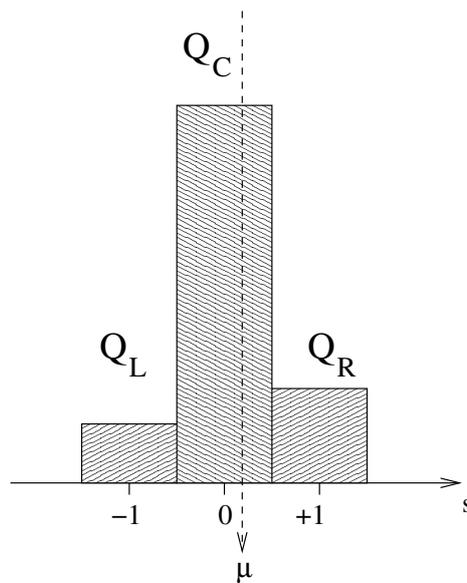


Figure 1: a notional sketch of the charge deposited on three consecutive strips. The horizontal axis is strip units,  $s$ , with the muon passing slightly to the right of zero. Three charges are registered,  $Q_L$ ,  $Q_C$  and  $Q_R$ , as shown.

115 than in chambers with small strips. For this reason, the strips in the  $ME_{\pm 1/1}$  chambers  
 116 have been made particularly small (cf. Table 1), since they play a key role in the momentum  
 117 measurement in the end caps [2].

118 Finally, a muon which passes through the anode plane at an oblique angle (with respect to  
 119 the strips) will produce a relatively broad distribution of charge across the gas gap, leading  
 120 to a smearing of the distribution of charges  $Q_L$  to  $Q_R$ , and a poorer resolution.

### 121 2.3 Qualitative Results from CRAFT

122 The CRAFT data provide an excellent opportunity to study the point resolution of the CSC's.  
 123 More than 300 M cosmic muon triggers were recorded, of which roughly 20% were generated  
 124 by the CSC's. It was necessary to further filter the CSC events to obtain a sample that was  
 125 useful for these studies.

126 An offline analysis package, `CSCResiduals`, was developed to investigate the point resolu-  
 127 tion of the CSC's. The code includes a filter to select events with good segments as well as  
 128 an analysis module.

129 Events were selected which contained a good segment from which residuals distributions for  
 130 layer 3 could be formed. A good segment was one which contained six rechits and  $\chi^2 < 200$   
 131 (unreduced). An event was selected if it contained at least one good segment. In order  
 132 to retain only clean events, any event with more than eight segment of any quality were  
 133 rejected, as well as events with more than fifty rechits. The event was also rejected if any  
 134 chamber contained more than four segments of any quality. A total of  $1.58 \times 10^3$  events was  
 135 selected from a subset of the CRAFT data, and about a third satisfied the further criteria  
 136 specified below. The numbers of segments available for each chamber type can be found in  
 137 Appendix A.

138 Further criteria were applied when filling residuals distributions, to ensure that the results  
 139 were based on the cleanest possible segments and hits:

- 140 1. the estimated errors on the six rechits has to be smaller than 0.2 strip widths. This  
 141 eliminates rechits based on a single strip or for which the cross-talk correction led to  
 142 negative values for  $Q_R$  and  $Q_L$ .
- 143 2. The sum of charges for three strips and three time slices for layer three could not be too  
 144 small or too large:  $250 < Q_{3 \times 3} < 1000$  ADC counts.
- 145 3. The segment inclination should correspond to tracks originating roughly from the in-  
 146 teraction point:

$$-1 < \frac{dy}{dz} < -0.15 \quad \text{and} \quad \left| \frac{dx}{dz} \right| < 0.15 \quad (5)$$

145 where these are local coordinates:  $dy/dz$  is the angle with respect to the anode wires,  
 146 and  $dx/dz$  is the angle with respect to the cathode strips. (See also Ref. [8].)

- 147 4. The strip coordinates were fit to a straight line. The resulting  $\chi^2$  value were required to  
 148 be less than 9 for the 5-hit fit, and less than 50 for the 6-hit fit.

149 These cuts were relaxed singly when checking the impact of these criteria. For further dis-  
 150 cussion of these basic criteria, see Appendix A.

151 In the remainder of this section, we use the CRAFT data to demonstrate the expected be-  
 152 havior as described in Section 2.2. No attempt was made to remove layer-by-layer misalign-  
 153 ments, as these are known to be small compared to the resolution.

### 154 2.3.1 Resolution as a Function of Charge

155 The “charge” depends on several factors, including the gas composition, pressure, high volt-  
 156 age, amplifier gain, and of course the ionization of the gas by the muon. We denote by  $Q_{3 \times 3}$   
 157 the sum of the charges recorded in three time bins across three consecutive strips [4, 7]. A  
 158 distribution of  $Q_{3 \times 3}$  for the CRAFT data is shown in Fig. 2. One ADC count in this figure  
 159 amounts to approximately XXXXXX pC. The distribution has a long tail, similar to that ex-  
 160 pected from the Landau distribution. The overall gain, including electronics gain, varies  
 161 considerably from chamber to chamber, however, so the distribution in Fig. 2 is more accu-  
 162 rately described as a sum of many Landau distributions, with widely varying peak positions.

163 Residuals distributions were made for several bins in  $Q_{3 \times 3}$  and fit individually to Gaussians.  
 164 A direct comparison of the residuals distributions is shown in Fig. 3, which shows plainly  
 165 that small charges give poorer resolution. One can also see that the very largest charges do  
 166 not give the very best resolution, due to distortions of the charge distribution caused by  $\delta$ -ray  
 167 electrons.

168 A summary of the variation of resolution as a function of charge is given in Fig. 4. Chambers  
 169 in rings  $ME \pm 2/2$  and  $ME \pm 3/2$  were selected for this plot, since they have the largest number  
 170 of events in CRAFT. The cuts on the  $\chi^2$  of the 2-dimensional strip fit were relaxed for this  
 171 study, so that the impact of  $\delta$ -ray electrons is clear. If the cuts are imposed, then the rise for  
 172  $Q_{3 \times 3} > 800$  ADC counts is eliminated.

In order to interpret the behavior seen in Fig. 4, we performed an *ad hoc* parametrization  
 of the observed variation of the resolution with charge, assuming that at low charge, the  
 variation goes as  $1/Q$ , that there is a constant term representing electronics noise and similar  
 effects, and that the poorer resolution caused by  $\delta$ -ray electrons rises linearly with charge.  
 Our *ad hoc* function <sup>4</sup> is:

$$\sigma(Q) = \sqrt{\left(\frac{a}{Q}\right)^2 + (b + cQ)^2} \quad (6)$$

173 where the parameters  $a$ ,  $b$  and  $c$  are to be determined by a fit. For the results shown in Fig. 4,  
 174 we obtain an excellent description with  $a = 11.6 \pm 0.2/(\text{ADC count})$ ,  $b = 0.018 \pm 0.001$  and  
 175  $c = (1.4 \pm 0.1) \times 10^{-5}$ .

176 Another demonstration of the sensitivity of the resolution to charge is provided by two runs  
 177 taken outside of the CRAFT exercise, in which the high voltage was raised by 50 V. Since the  
 178 number of events was modest, the event and segment selection was somewhat looser than  
 179 described above. Fig. 5 shows the increase in the charge and the consequent improvement  
 180 in the resolution. The improvement is consistent with the expected  $1/Q$  behavior.

### 181 2.3.2 Resolution as a Function of the Position Within a Strip

182 The resolution obtained from the measurement of  $Q_L$ ,  $Q_C$  and  $Q_R$  is much better than if  
 183 one simply put the hit at  $s = 0$  and set the uncertainty to the strip width divided by  $\sqrt{12}$ .  
 184 Nonetheless, the strip width does play a central role, as discussed briefly in Section 2.2. If

<sup>4</sup>The error calculations in the reconstruction code take into account variations of the resolution with charge, as well as with strip width and the position within a strip. The function displayed in Eq. 6 is not used.

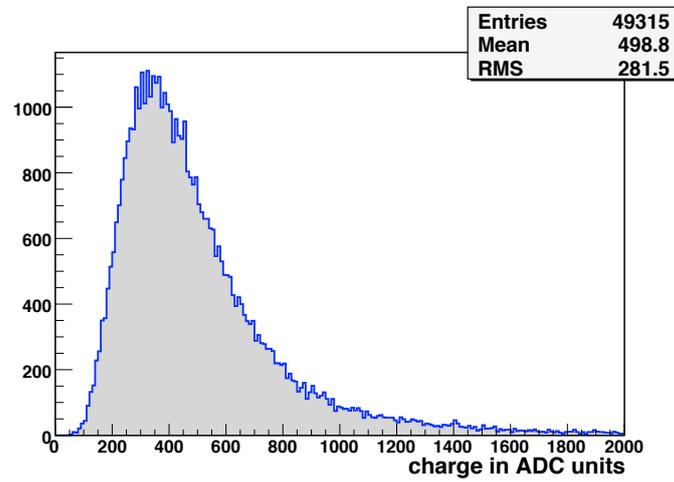


Figure 2: observed charge distribution,  $Q_{3\times 3}$ , in ADC counts.

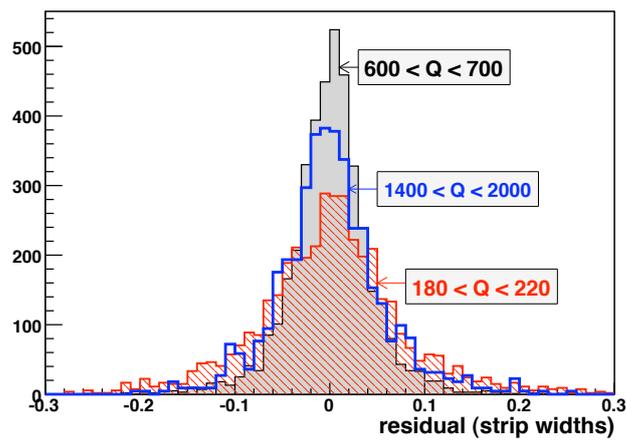


Figure 3: example residuals distributions, for three narrow ranges of charge. All three distributions are normalized to the same area

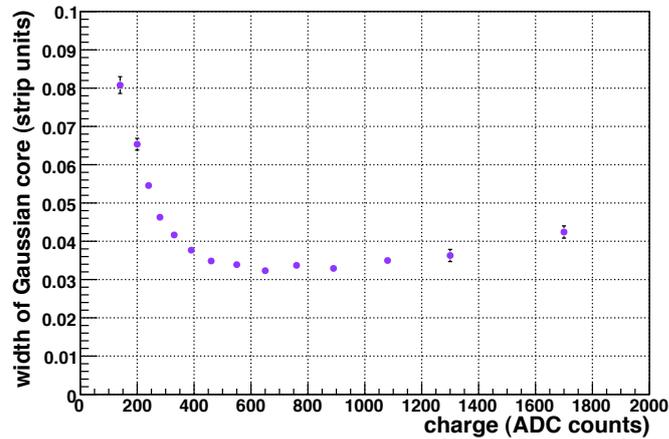


Figure 4: variation of the *per layer* resolution as a function of  $Q_{3 \times 3}$ . This measurement was made using chambers in  $ME_{\pm 2/2}$  and  $ME_{\pm 3/2}$ ; other chambers give very similar results.

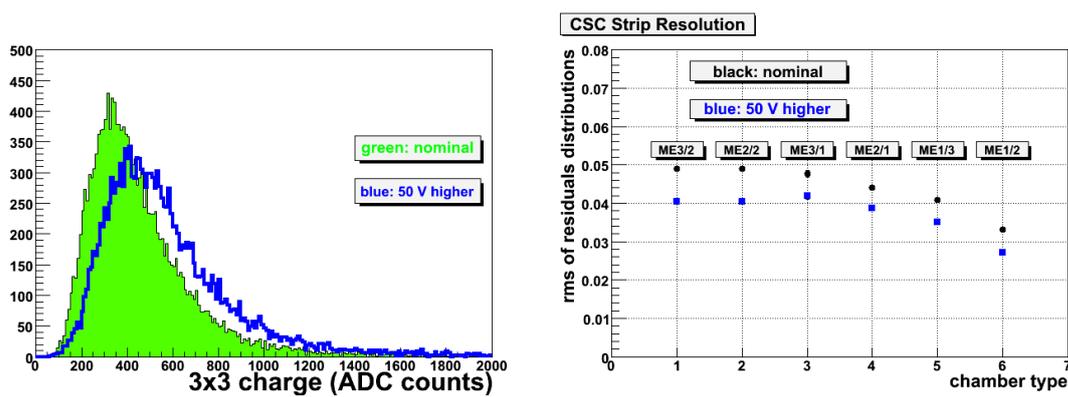


Figure 5: *Left*: charge distributions for two consecutive runs. The solid histogram corresponds to the nominal setting, and the open histogram corresponds to an increase of 50 V. *Right*: comparison of the resolution for the same two runs.

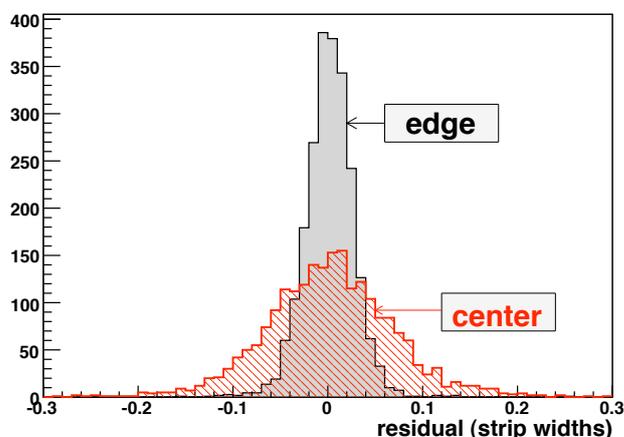


Figure 6: example residuals distributions, for muons passing near the center and near the edge of the strip

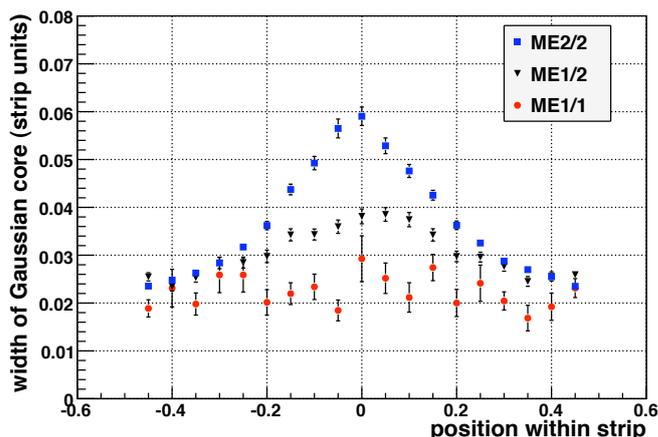


Figure 7: variation of the *per layer* resolution as a function of  $s$ , the position within the strip, for three different types of chambers

185 the charge is nearly the same on two consecutive strips, then the measurement is optimal;  
 186 it is worse when the minimum charge is measured on the side strips. A direct comparison  
 187 of the residuals distribution for two extreme cases is shown in Fig. 6. The distribution for  
 188  $|s| < 0.025$  (“center”) is much broader than the one for  $|s| > 0.425$  (“edge”).

189 A summary of the variation of the resolution with  $s$  is shown in Fig. 7. For the  $ME\pm 2/2$   
 190 chambers, the resolution in the center of the strip is worse by about a factor of two than at  
 191 the edge. This variation is weaker for chambers with thinner strips, such as  $ME\pm 1/2$  and  
 192  $ME\pm 1/1$ .

### 193 2.3.3 Resolution as a Function of the Strip Width

194 Most of the analysis is done in terms of the normalized strip width,  $s$ . The physical width  
 195 of the strip matters, too. For broad strips, most of the charge is collected on the central strip,

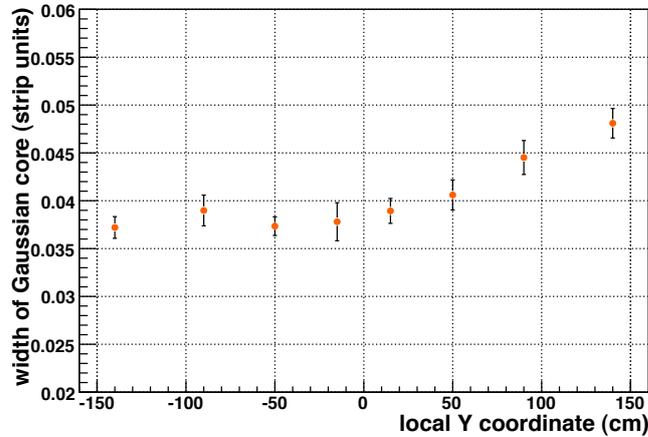


Figure 8: variation of the *per layer* resolution as a function of  $y$ , the local coordinate roughly parallel to the strips. These measurements were done with the  $ME\pm 2/2$  and  $ME\pm 3/2$  chambers.

196 leaving a small amount for  $Q_L$  and  $Q_R$ , leading to a poorer resolution. For this reason, the  
 197 smaller chambers have a much better resolution than the larger chambers. Within a chamber,  
 198 there is a variation of the resolution along the strip, since the strip is narrower at the narrow  
 199 end of the chamber ( $y < 0$ ) and wider at the broad end ( $y > 0$ ). Fig. 8 illustrates this behavior  
 200 for chambers from  $ME\pm 2/2$ .

### 201 2.3.4 Resolution as a Function of the Track Angle

202 The results in the previous subsections were derived for muon trajectories that were nearly  
 203 perpendicular to the strips. For low-momentum muons coming from the interaction point,  
 204 however, more oblique trajectories are possible. We have observed a clear variation of the  
 205 resolution as a function of  $dx/dz$  in chambers from ring  $ME\pm 2/2$ , see Fig. 9. For all other  
 206 results reported in this note, a tight cut on  $|dx/dz|$  has been applied.

### 207 2.3.5 Normalized Residuals

208 The rechit code computes the estimated uncertainty taking variations as a function of charge,  
 209 position within a strip, and strip width into account [7]. Distributions of normalized residu-  
 210 als (“pull distributions”) allow us to check those calculations.

211 Fig. 10 shows the pull distribution for all chambers. The shape is fairly Gaussian, and the  
 212 fitted width is  $\sigma = 1.349 \pm 0.005$ , which is fairly close to the target value of 1.15. A summary  
 213 of the pulls for all chamber types is given in Table 2. Overall, the pulls are too wide, especially  
 214 for the  $ME\pm 1/1$  chambers. It will be possible to adjust the error estimates on the basis of the  
 215 CRAFT data.

### 216 2.3.6 Badly Reconstructed Segments

217 Most of the analysis presented in this note is directed toward the characterization of good  
 218 segments reconstructed from good rechits. Some rechits are quite poor, however, and some  
 219 segments have a very large  $\chi^2$ . In this subsection, we present some investigations of these  
 220 cases.

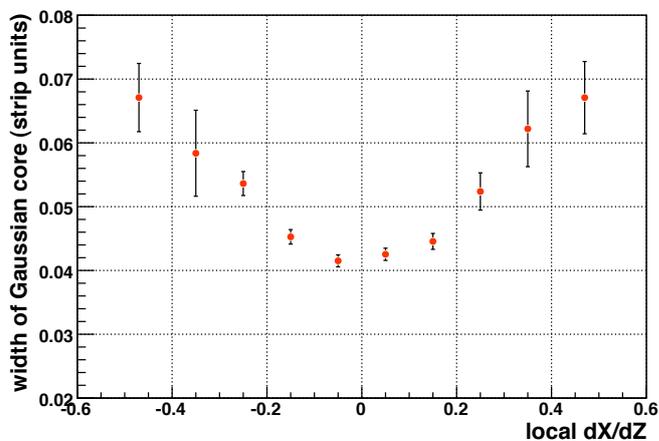


Figure 9: variation of the *per layer* resolution as a function of local  $dx/dz$ , which quantifies the segment inclination with respect to the strips. These measurements were done with the  $ME\pm 2/2$  chambers.

ring	width of pull distribution
$ME\pm 1/1b$	$1.89 \pm 0.06$
$ME\pm 1/2$	$1.34 \pm 0.01$
$ME\pm 1/3$	$1.52 \pm 0.01$
$ME\pm 2/1$	$1.28 \pm 0.02$
$ME\pm 2/2$	$1.42 \pm 0.01$
$ME\pm 3/1$	$1.26 \pm 0.04$
$ME\pm 3/2$	$1.37 \pm 0.02$
$ME\pm 4/1$	$1.17 \pm 0.03$

Table 2: widths of the normalized residual distributions, obtained by fitting the central core of the distribution, as in Fig. 10.

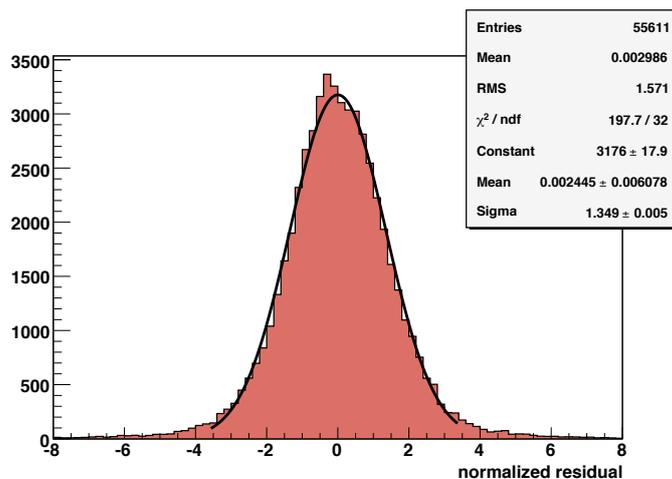


Figure 10: distribution of normalized residuals (“pull distribution”) for all chambers. Also shown is a fit to a single Gaussian.

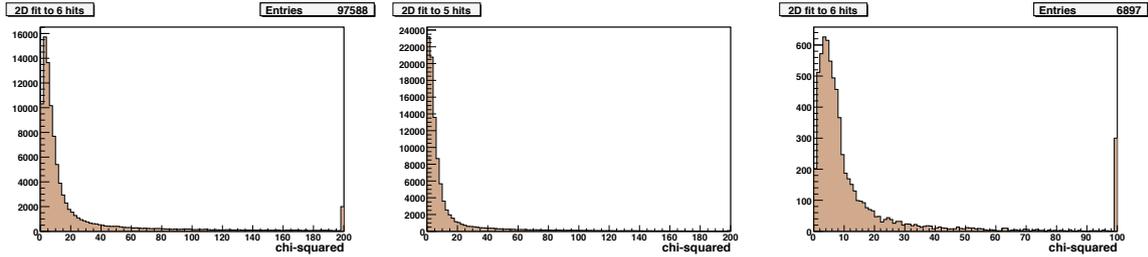


Figure 11: distributions of  $\chi^2$  values obtained by fitting the strip coordinates to straight lines. *Top*:  $\chi^2_{(6p)}$  after all selection but before cuts on  $\chi^2$ . *Middle*:  $\chi^2_{(5p)}$ . A tight cut is placed at  $\chi^2_{(5p)} < 9$ . *Bottom*:  $\chi^2_{(6p)}$  after the tight cut on  $\chi^2_{(5)}$ . A loose cut is applied:  $\chi^2_{(6p)} < 50$ .

221 The bottom plot in Fig. 11 shows  $\chi^2_{(6p)}$  after a tight cut on  $\chi^2_{(5p)}$ . The long tail is caused by bad  
 222 rechits in layer 3. We applied a cut  $\chi^2_{(6p)} > 100$  to select a sample of about 300 such rechits.  
 223 Fig. 12 shows some interesting distributions for these bad rechits.

224 The first plot shows the pull distribution. Given the way these bad rechits were selected,  
 225 one expects large values with an absence of small values. The next plot shows the actual  
 226 residuals, which also have a hole and somewhat, but not very large values. The third plot  
 227 shows that the estimated errors are quite tiny – compare with Fig. 15 which shows much  
 228 larger values for more normal rechits. Thus the large pulls are caused mainly by small es-  
 229 timated errors. The fourth plot gives a clue why the errors might be small: the measured  
 230 charge is very large – compare to Fig. 2. The very large charge may indicate a  $\delta$ -ray electron  
 231 or some other agent distorting the pulses on the strips. Another clue comes from the last  
 232 plot, showing that the “bad” rechits are found more often near the edge of the strip, where  
 233 the error should be smaller. The reconstruction code computes the estimated errors based on  
 234 average behavior of the resolution as a function of charge, position within the strip and strip  
 235 width. Apparently, for these peculiar rechits, there is a conspiracy of effects, namely very  
 236 large charge, and a position close to the edge of a strip.

237 In short, for rechits near the edge of a strip, when the charge is very high, the measured  
 238 coordinate might be less accurate, and the estimated error too small, leading to a very large  
 239 normalized residual and a bad value for  $\chi^2$ .

## 240 2.4 Measurements of the Nominal Resolution

241 The results in the previous section demonstrate the expected qualitative behavior of the res-  
 242 olution. In this section, we quantify the resolution of the CSC’s, as measured with CRAFT  
 243 data, in order to verify that they are performing as designed.

244 The cut  $\chi^2 < 200$ , listed in Section 2.3, is a loose cut, which could allow segments in which  
 245 the fit to rechits in layers 1, 2, 4, 5 & 6 might give a poor prediction for the position in layer 3.  
 246 This is why we impose a tight cut on  $\chi^2_{(5p)}$  for the 5-hit, 2-dimension fit to all strips except  
 247 the one from which we will obtain the residuals distribution. We studied the impact of the  
 248 cut on  $\chi^2_{(5p)}$  by selecting segments in  $ME \pm 2/2$  for which  $|s| > 0.4$  in layer 3, and checking  
 249 the width of the residuals distribution as the cut on  $\chi^2_{(5p)}$  was tightened. See Appendix A for  
 250 more information. A very loose cut is placed on  $\chi^2_{(6p)}$  to remove rechits which are far off the  
 251 correct position.

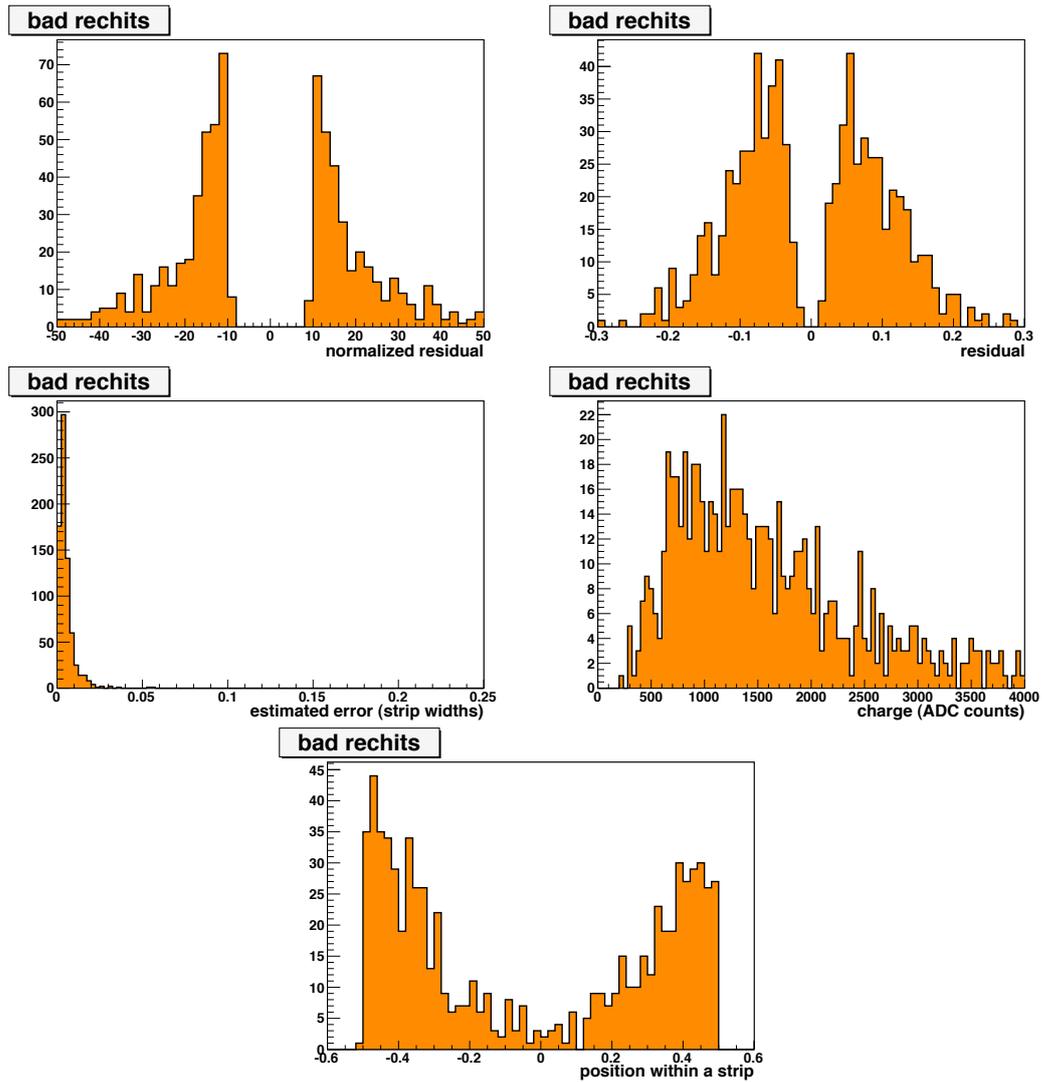


Figure 12: distributions for rechits giving  $\chi^2_{(6p)} > 100$ .

ring	resolution			
	fit to two Gaussians		derived from $\chi_0^2$	
	strip widths	$\mu\text{m}$	strip widths	$\mu\text{m}$
ME $\pm$ 1/1b	$0.024 \pm 0.002$	144	0.017	102
ME $\pm$ 1/2	$0.034 \pm 0.001$	285	0.029	245
ME $\pm$ 1/3	$0.044 \pm 0.001$	578	0.041	537
ME $\pm$ 2/1	$0.046 \pm 0.001$	510	0.044	489
ME $\pm$ 2/2	$0.040 \pm 0.001$	487	0.039	474
ME $\pm$ 3/1	$0.054 \pm 0.002$	633	0.052	613
ME $\pm$ 3/2	$0.044 \pm 0.001$	534	0.041	501
ME $\pm$ 4/1	$0.054 \pm 0.004$	648	0.052	625

Table 3: resolution *per layer* for each chamber type.

ring	resolution ( $\mu\text{m}$ )		
	design	<i>per layer</i> / $\sqrt{6}$	Eq. 2
ME $\pm$ 1/1	75	59	53
ME $\pm$ 1/2	75	116	110
ME $\pm$ 1/3	150	234	194
ME $\pm$ 2/1	150	208	172
ME $\pm$ 2/2	150	199	169
ME $\pm$ 3/1	150	258	200
ME $\pm$ 3/2	150	218	182
ME $\pm$ 4/1	150	264	221

Table 4: resolution *per chamber* for each chamber type

252 Residuals distributions for chambers in each ring were fit to the sum of two Gaussians, and  
 253 the resolution computed according to Eq. 1. These distributions and the fits are given in  
 254 Appendix B. Table 3 lists the *per layer* resolution obtained in this manner. The values given  
 255 in  $\mu\text{m}$  are obtained by multiplying the resolution in strip widths by the average width of the  
 256 strip (see Table 1).

257 We formed distributions of  $\chi_0^2$  (Eq. 3) for each chamber type – some examples are given in  
 258 Fig. 13. We computed  $\sigma_0$  (which would be in units of the strip width) and converted to an  
 259 uncertainty in  $\mu\text{m}$  using the average physical strip width. The results are listed in Table 3.  
 260 These values are somewhat smaller than the values obtained from the fit to two Gaussians.

261 The resolution of a chamber, given six good rechits, can be estimated on the basis of the *per*  
 262 *layer* resolution. One can simply take the numbers listed in Table 3 and divide by  $\sqrt{6}$ , or one  
 263 can perform a slightly more refined analysis indicated by Eq. 2. The latter gives systemati-  
 264 cally lower values for the resolution than the former. Table 4 lists both sets of values, which  
 265 can be compared to the design values [2]. In general, the observed values are somewhat  
 266 higher, due in part to the 10% inflation inherent in the method, and from the fact that the  
 267 high voltage setting is slightly lower than nominal.

268 Very similar studies have been conducted by the DUBNA group and are available already  
 269 in Ref. [12]. Their selection of segments is somewhat tighter than what has been described  
 270 here. For example, they applied much tighter cuts to the  $\chi^2/\text{NDF}$  for the segment fit, and  
 271 also for the 6-hit 2-dimension strip fit, here denoted  $\chi_{(6p)}^2$ . From CRAFT data they obtained a

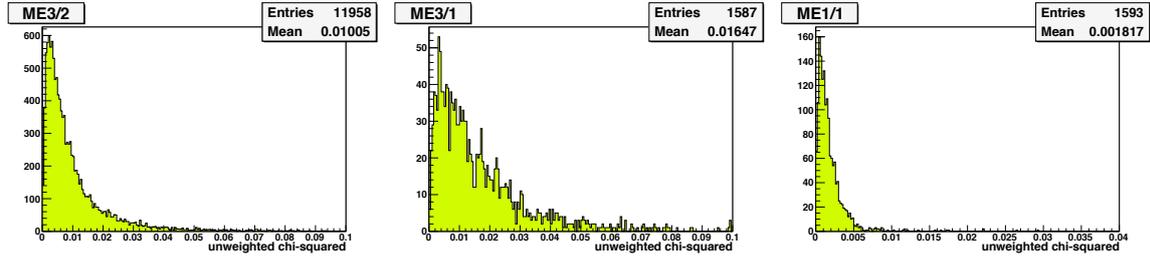


Figure 13: example distributions of  $\chi_0^2$

272 *per layer* resolution of  $107 \mu\text{m}$  for ME1/1, and a *per chamber* resolution of better than  $50 \mu\text{m}$ .  
 273 These values are not incompatible with those listed in Tables 3 and 4. For the details of their  
 274 study, see Ref. [12].

### 275 3 Conclusions

276 The CRAFT data have been used to study the resolution of the CSC's as a function of charge,  
 277 position within a strip, strip width, and track angle, as well as to quantify the resolution  
 278 of all chamber types. The expected qualitative behavior has been demonstrated. The mea-  
 279 sured resolutions of all chamber types compare reasonably well with the design values, as  
 280 tabulated in Table 4, given the fact that the high voltage is set lower than originally intended.

281 More refined studies can be carried out in the future, either with cosmic ray muons, or,  
 282 hopefully, with muons produced in  $pp$  collisions.

### 283 Acknowledgments

284 The approach and direction of these studies take inspiration from the earlier work by Stan Durkin  
 285 (OSU) [5]. The fine work by the Florida Group also set an excellent example [4].

### 286 Appendix A

287 Justifications for the criteria listed in Section 2.3 are given below, based on distributions made  
 288 from the output of a loose CSC skim (program `CSCSKIM`, skim type 1). This skim demanded  
 289 at least three chambers with hits, and at least two segments of any quality.

290 Fig. 14 shows the distribution of the total number of rechits in an event. Spikes correspond-  
 291 ing to one, two and three chambers are visible. Four chambers correspond to 24 hits, except  
 292 when one of them is  $\text{ME}\pm 1/1a$ , in which case the number is 48. The cut is placed at 50.  
 293 Events with very many segments come from showers, which clearly are inappropriate for  
 294 these studies. A rather loose cut at 8 has been placed. Similarly, no chamber may have more  
 295 than four segments. This excludes the possibility that a single chamber has a number of rechits  
 296 close to 60, leading to very many three-hit segments that do not correspond to a muon  
 297 track.

298 Given that most “messy” events are eliminated by these three cuts, we can look at the quality  
 299 of the remaining segments. Fig. 14 shows the number of hits on a segment; we require six.  
 300 After that cut is applied, the unreduced  $\chi^2$  distribution shows a reasonable peak around 8,

301 with a very long tail. The plot puts all overflow entries in the bin just before 200 – these  
 302 are the segments that are eliminated. These segments would also be reduced by the cut on  
 303 the estimated hit errors, discussed below. Given these two cuts defining a “good” segment,  
 304 the number of good segments per event is also shown. Most events contain more than one  
 305 good segment, indicating that these events correspond to valid muon trajectories that are  
 306 reconstructed well.

307 If a segment has a hit with a large uncertainty, then the segment may be unreliable, so such  
 308 segments are rejected. Fig. 15 shows the distribution of the largest uncertainty of all the  
 309 hits on a segment. A clear spike at  $1/\sqrt{12} = 0.289$  is visible. Our criteria demand that this  
 310 uncertainty be less than 0.2. For reference, Fig. 15 also shows the distribution of uncertainties  
 311 for the hits in layer 3.

312 The prediction of the coordinate in layer 3 is likely to be poor if the 5-hit fit to layers 1, 2, 4,  
 313 5 & 6 has a bad  $\chi^2_{(5p)}$ . Successively tighter cuts on  $\chi^2_{(5p)}$  were tried, and a stable resolution  
 314 obtained for  $\chi^2_{(5p)} < 10$ . After this cut is applied, the incidence of extremely bad residuals is  
 315 reduced by applying a loose cut on the 6-hit  $\chi^2_{(6p)}$ , namely  $\chi^2_{(6p)} < 50$ . Distributions of  $\chi^2_{(5p)}$   
 316 and  $\chi^2_{(6p)}$  are shown in Fig. 11.

## 317 Appendix B

The residuals distributions for all chamber types are given in this appendix. The distribu-  
 tions have been fit to sums of two Gaussians, with means set to zero. The function form  
 is:

$$f(x) \equiv \frac{A_1}{\sqrt{2\pi}\sigma_1} \exp\left(\frac{-x^2}{2\sigma_1^2}\right) + \frac{A_2}{\sqrt{2\pi}\sigma_2} \exp\left(\frac{-x^2}{2\sigma_2^2}\right) \quad (7)$$

318 where optimal values for the parameters  $\sigma_1$ ,  $\sigma_2$ ,  $A_1$  and  $A_2$  are obtained from the fit. The  
 319 resolution is defined by Eq. 1. The residuals distributions with fits are given in Fig. 16.

320 Another test of the position measurement is provided by the distribution of the strip coordi-  
 321 nates themselves. Ideally, this distribution should be a flat-top box for  $-0.5 < s < 0.5$ .  
 322 Resolution on  $s$  will round off of sides of the box. Also, some rechits coordinates cannot be  
 323 calculated correctly, if one does not have three strips (sometimes there are two few or even  
 324 too many) or if the cross-talk correction leads to negative values for  $Q_L$  and/or  $Q_R$ . Fig. 17  
 325 shows the distributions of  $s$  for all chamber types.

326 For reference, a summary of the mean charge  $\langle Q_{3\times 3} \rangle$  and r.m.s. pedestal width is given in Ta-  
 327 ble 5. These numbers come from run quality monitoring plots produced using `CSCValidation` [13].

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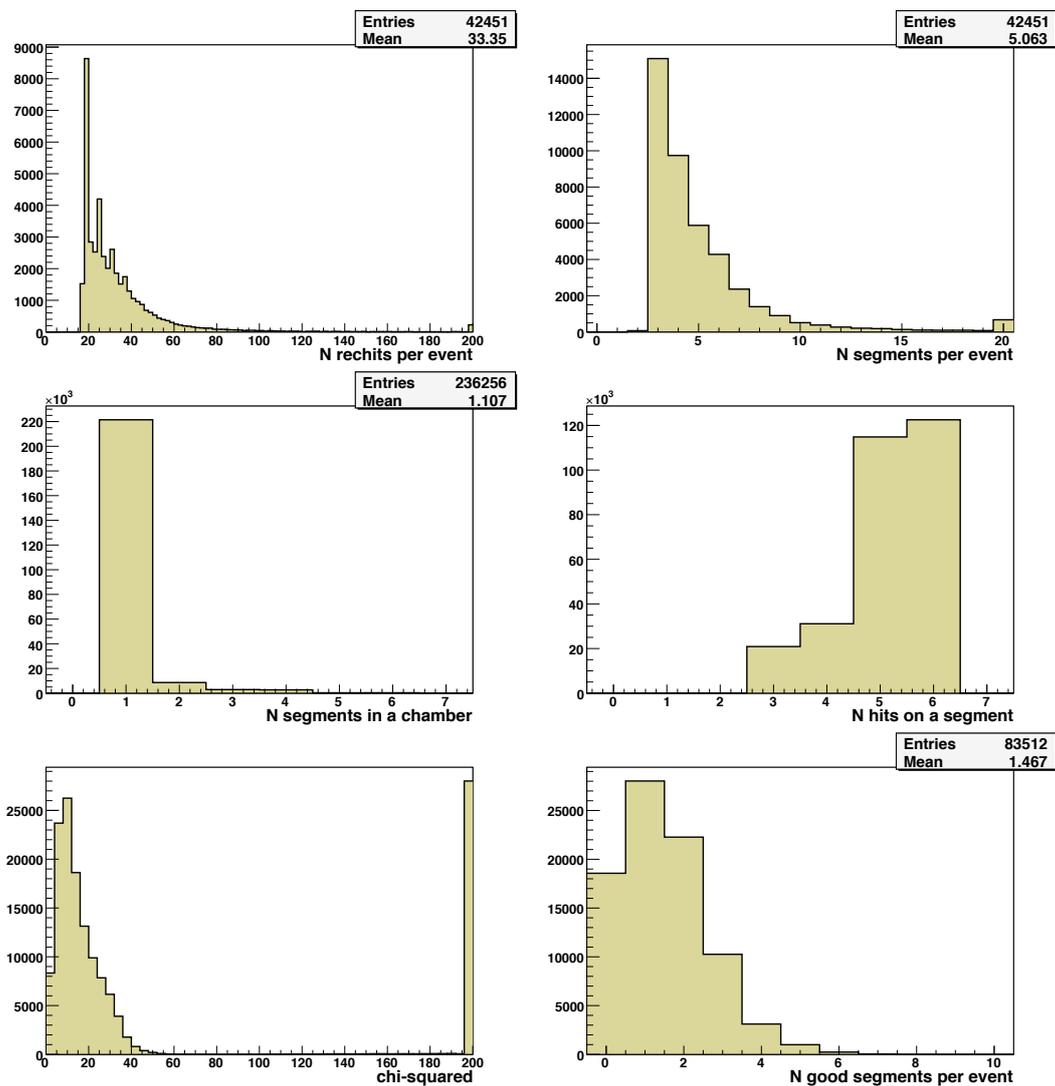


Figure 14: distributions of basic quantities used in event selection

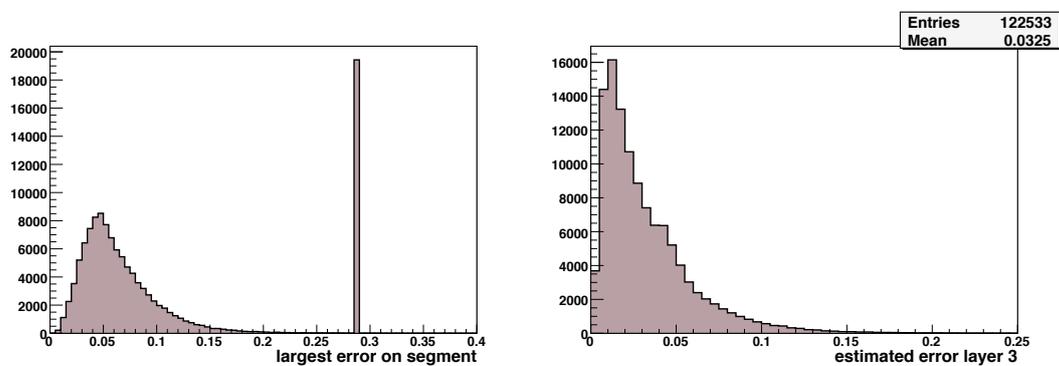


Figure 15: *Left:* largest estimated error for all rechits on a segment. A segment is rejected if this largest error is larger than 0.2. *Right:* the estimated error for selected rechits in layer 3.

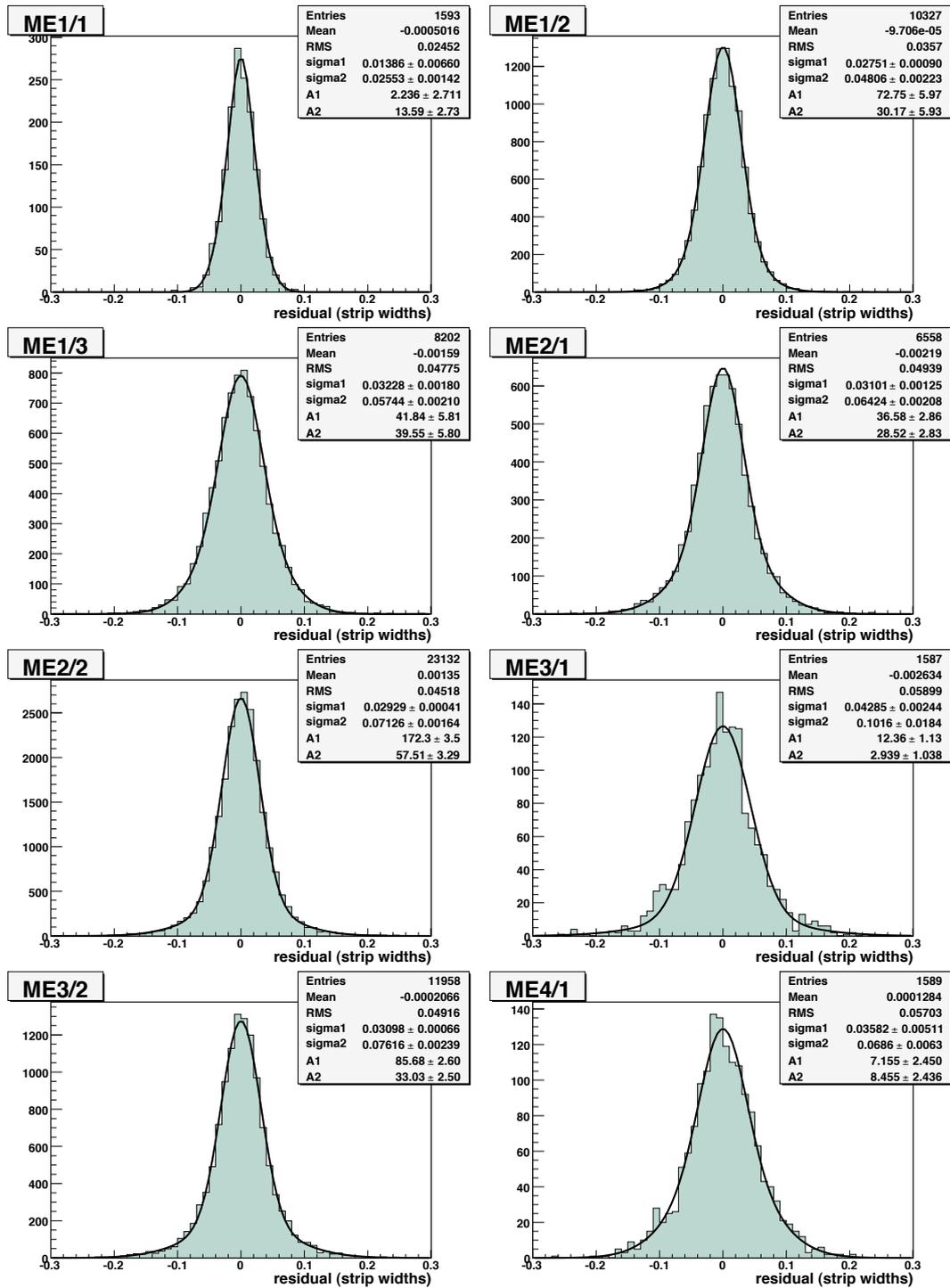
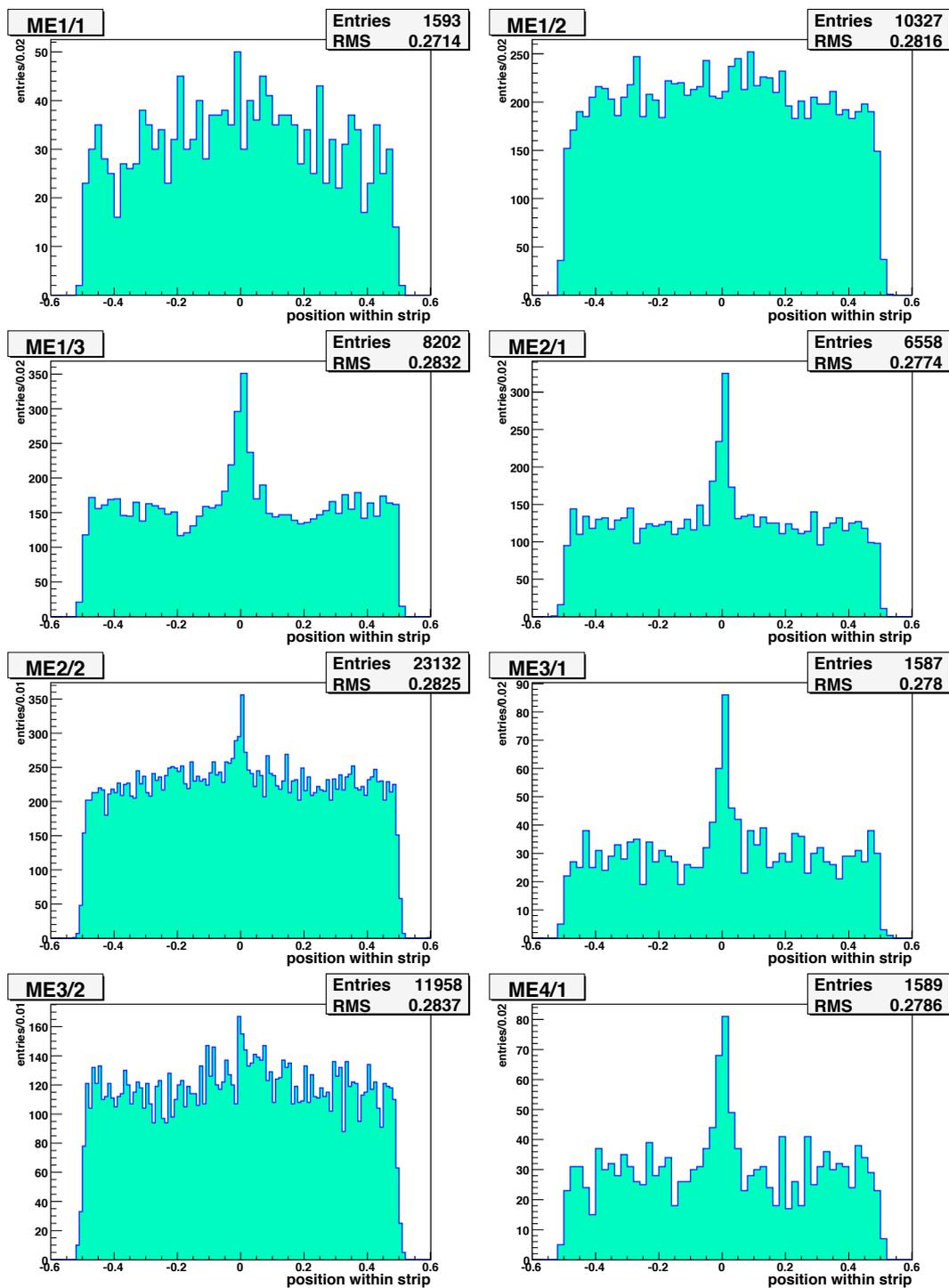


Figure 16: residuals distributions fit to the double-Gaussian function given in Eq. 7.

Figure 17: distributions of strip coordinates,  $s$ , for all chamber types

chamber	$\langle Q_{3 \times 3} \rangle$	r.m.s. pedestal width
ME $\pm$ 1/1	926	2.26
ME $\pm$ 1/2	796	2.00
ME $\pm$ 1/3	822	2.27
ME $\pm$ 2/1	745	2.08
ME $\pm$ 2/2	782	2.80
ME $\pm$ 3/1	723	2.05
ME $\pm$ 3/2	784	2.81
ME $\pm$ 4/1	724	1.93

Table 5: mean  $Q_{3 \times 3}$  and the r.m.s. pedestal width, ascertained from `CSCValidation` plots for CRAFT run 68100. Numbers are in ADC counts.

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